## Mapping on reference genomes



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### Literature

Mapping short DNA sequencing reads and calling variants using mapping quality scores. Li et al. Genome Research (2008) doi: 10.1101/gr.078212.108 (MAQ)

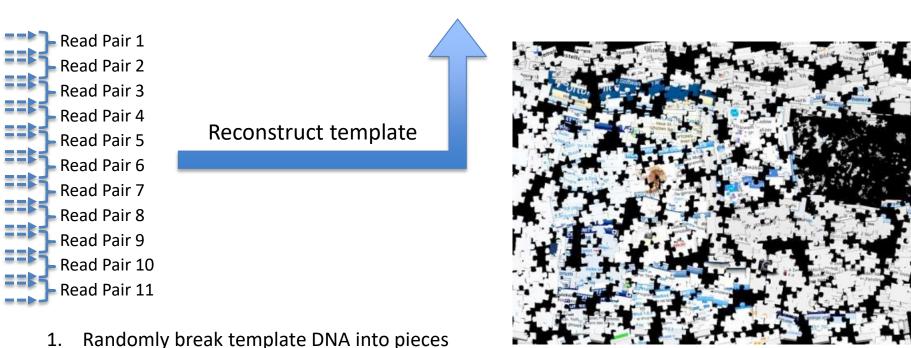
Ultrafast and memory-efficient alignment of short DNA sequences to the human genome. Langmead et al. Genome Biology (2009) doi:10.1186/gb-2009-10-3-r25 (BOWTIE)

Mapping Reads on a Genomic Sequence: An Algorithmic Overview and a Practical Comparative Analysis
Schbath et al. Journal of computational biology (2012)
doi:10.1089/cmb.2012.0022 (Review)

NextGenMap: fast and accurate read mapping in highly polymorphic genomes. Sedlazeck et al. Bioinformatics (2013) doi:10.1093/bioinformatics/btt468 (NextGenMap)

## REFERENCE BASED MAPPING

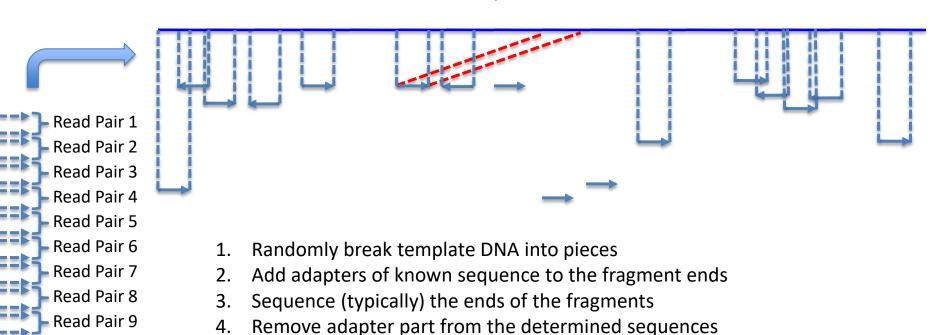
## Strategies to sequence long DNA molecules: Shotgun sequencing



- Add adapters of known sequence to the fragment ends
- 3. Sequence (typically) the ends of the fragments
- Identify and remove adapter part from the determined sequences
- Reconstruct template sequence from the sequence reads

# Strategies to sequence long DNA molecules: Shotgun sequencing and **reference guided** sequence assembly

#### Reference Sequence



- 5. Reconstruct template sequence from the sequence reads
  1. Reference guided sequence assembly: map reads to
  - 1. Reference guided sequence assembly: map reads to a reference sequence. Note that reads can map equally good to more than one position in the reference genome, e.g. due to repeats in the reference.

#### Reference sequence

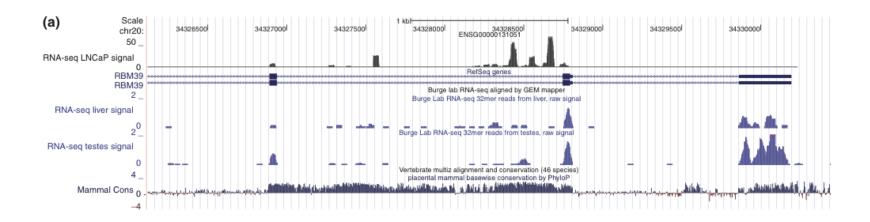
Read Pair 10

Read Pair 11

- a) e.g. genome of a different individual from the same species to study species diversity
- b) e.g. genome of a closely related species

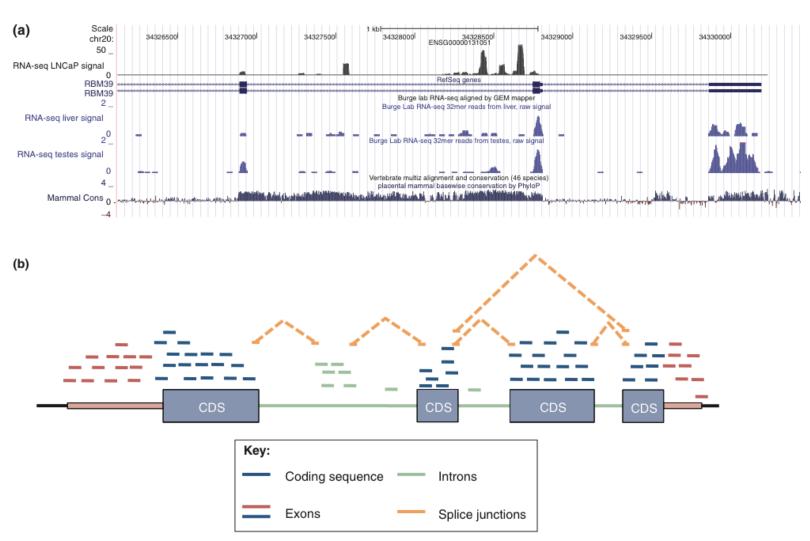


## Short Read Application: RNA seq mapping





# RNA-seq mapping helps building hypotheses concerning gene structure



from Oshlack et al. Genome Biology 2010, 11:220

### **Short Read Applications**

• Genotyping

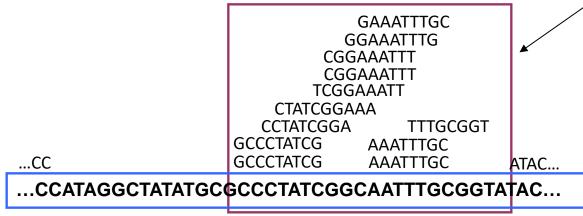
— CCATAG TATGCGCCC CGGAAATTTCGGTATAC
— CCAT CTATATGCG TCGGAAATT CGGTATAC
— CCATGGCTATATG CTATCGGAAA GCGGTATA
— CCAAGGCTATAT CCTATCGGA TTGCGGTA C...
— CCAAGGCTATAT GCCCTATCGAAATTTGC ATAC...
— CCTAGGCTATAT GCCCTATCGAAATTTGC GTATAC...
— CCTAGGCTATATGCGCCCTATCGAAATTTGC GTATAC...

— CCATAGGCTATATGCGCCCTATCGGCAATTTGCGGTA

TAC...

Goal: classify, measure significant peaks

RNA-seq, ChIP-seq, Methyl-seq, Ribo-seq



### Challenges

- mapping millions/billions of reads to a large genome is hard:
  - how quickly can we map the reads to the genome?

– how do we deal with multiple mapping positions?

 how do we deal with sequencing errors and genetic divergence/diversity

– how do we deal with reads that span intron-exon boundaries?

## **SHORT READ ALIGNMENT**

### Short Read Alignment

- Given a reference and a set of reads, report at least one "good" local alignment for each read if one exists
  - Approximate answer to: from where in genome did the read originate?

### What is "good"?

- Fewer mismatches is better
- Failing to align a low-quality base is better than failing to align a high-quality base

```
...TGATCATA...
dAtcat
better than ...TGATCATA...
dAGAAT
...TGATATTA...
dAtcat
better than ...TGATCATA...
dATCATA...
dATCATA...
dTACATA...
dTACAT
```

## Genome to search in: AATGAGACATGAA

#### Reads to search:

Query1: CATG

Query2: ATGT

Genome: AATGAGACATGAA

Query1: CATG



1234567891234 Searchstring: AATGAGACATGAA

CATG ----

Just slide the word along the sequence and stop when either end of sequence is reached or mapping position is found.

Genome: AATGAGACATGAA

Query1: CATG



1234567891234
Searchstring: AATGAGACATGAA

CATG ----

Just slide the word along the sequence and stop when either end of sequence is reached or mapping position is found.

Genome: AATGAGACATGAA

Query1: CATG



1234567891234 Searchstring: AATGAGACATGAA

CATG ———

Just slide the word along the sequence and stop when either end of sequence is reached or mapping position is found.

Genome: AATGAGACATGAA

Query1: CATG



1234567891234

Searchstring: AATGAGACATGAA

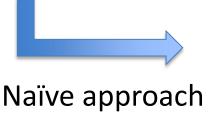


Query1 maps to position 8-12 in Genome

Full match found, Output result

Genome: AATGAGACATGAA





1234567891234

Searchstring: AATGAGACATGAA



At most n-k comparisons, with n is the length of the search string, and k is the query length (read length).

This is not feasible for short read mapping.

### Run Time of the Naïve approach

#### Naive approach:

- O(L<sub>G</sub> L<sub>r</sub> N<sub>r</sub>)
- $L_G \rightarrow$  Size of the genome sequence
- $L_r \rightarrow Size of the read$
- $N_r \rightarrow$  Number of the reads

#### Allowing gaps:

- Needleman Wunsch as dynamic programming algorithm
- Same complexity O(L<sub>G</sub> L<sub>r</sub> N<sub>r</sub>)

### Indexing speeds up searches

#### INDEX Collins, Clemmons Adams, Jesse Conover, Benjamin Edward 61 Alvarado, Hiram O. 46, 138 Conover, B. F. Frio County Centennial Arnold, Dan and Benina Frio County Historical Conover, Freddie Marvin Arnold, George and Commission Conover, Fred N. Agatha 47 Frio County History Conover, George W Arnold, Henry and Cora Conover, George Washington Frio County Markers Assembly of God Church Frio County Time Capsule Conover, Mac D. Conover, Minnie Frio Pioneer Jail Museum Assembly of God Church Frio Public Library Conover, William O. (Pearsall) County, Roosevelt and Lois Fudge, Albert Lester Avant, Forrest J. 70-71 Cowden, George Gever, E. F. Avant, James Ross 71-72 Goodman, Nancy Johnson Cowley, W. B. Avant, Robert F. and Gross, L. E. Cox, Joseph Florrie Crawford, V. T. and Mary Gill Hugh E. Beall, Dr. J. E. 72 Grueser, Winifred Crocker, Minnie Bennett, John Crossette, Joanne Hardcastle, Henry J. Berry, James E. Harrell, William D. 11 Cude Frank Berry, Mrs. James E. Cude Lowell Harris, W. A. and Nancy Betts, Nena Ward Cude, Willis Franklin Harris, I. Will Bigfoot Baptist Church Dalkowitz, Harry and Evelyn Harris and Hindes Bigfoot Church of Havnes, Wynn Worsham Christ Danchak, John MIchael Henson, William F. Bigfoot Methodist Danchak, Joseph Franklin 74-75 Herron, James Church Higdon, George J. Davneport, Mary Bilhartz, August and 83 75-76, 150 Higdon, Grady and Ruth DeVilbiss, Luther 26-27 DeWoody, Alonzo Bilhartz, Joseph and DeWoody, T. V. Hortense B. Dillard, Nathan Blackaller, James 85 Dilley Church of Christ Hiler, James H. Harrison Dilley Presbyterian Church Hiler, Lee Reavis 85-86 65-66 Boon, William Dromgoole, Glenn A. and Hinojosa, Miguel Boswell, Miss Bird Holland, Albert Green Minnie L. 9-10 Boyd, William A. Holmes, Joseph M. 11-12 Dubose, Ruby K. Braun, John George 45-46 Howard, Dr. and Mrs. E. M. Dunn, Claude Bernard 66-67 Breazeale, Morris H Howard, Earl Winfield Dunn, Hubert Brown, Bernard \* 20-21, 137 32-33 Dunn, John Anthony Howerton, James 21 Brown, Charles A. Dunn, Oscar James Immaculate Heart of Mary Brown, Frank S. Dunn, Patrick Brown, James Gideon Jeffries, William Edwards, Eliza H. Crain 22 Brown, Milton B. 88-89 Edwards, Levi J. Wangruder Johnson, Quill Brown, Paul P. Jones, Charles Calvin Elkins, J. W. Busby, Alex and Gladys 89 Jones, Floyd G. Ellis, Houston H. Busby, Claude L. lones, G. B. and Michealna 89-90 Ellis, S. H. Busby, Robert 30 141 ones, James Marion Ellis, W. W. Busby, Roy and Lucilie ones, Jeremiah Denman 90 Fargason, Cloud O. Campbell, Alta 90, 150 Fargason, John E., Jr. and ones, Michael Joe (Mike) Campo, Luis Jordan, Sam H. Mildred Carmichael, Rev. Walter Fargason, John E., Sr. Karnes, Blanche Crawford Carroll, Barney R. Kemper, John Fields, John E. Carroll, Charles L. Kimball, Rev. James Floyd 92-93 First Baptist Church Carroli, James Henry King, J. J. and Mabel 33-34, 143 (Dilley) Carroll, Josephine and Klopek, Albert and Lucille First Baptist Church Geneva (Pearsall) Lee, Charles Edward Carroll, Louie Joseph, Ir. 50,51 First Christian Church Lester, Owen E. Carroll, Louie Joseph, Sr. 93-94 Lindholm, John Nelson (Pearsall) Carroll, Paul Eugene First United Methodist Lindholm, Mady Carroll, Wesley Raymond 94-95 Lippard, David Church (Dilley) Carroll, Wesley Robert 95 First United Methodist Little, Brice Carroll, William Patrick 51 Littleton, Sam and Ora Church (Pearsall) Cavender Family 95-96 Fitch, R. D. Long, R. G. Church of Christ (Pearsall) Lowe, Judge Marcellus Flores, Ted Clausewitz, Martin Foreman, Barton and Bessie Lyons, Arthur E. Coleman, Robert 78-79, 142 Malone, John J. Collins, John W. (Bill) Foster, Lorena

#### Indexing:

- Allow targeted search
- Genome distributed in chapter / keywords

#### Indexing speeds up searches

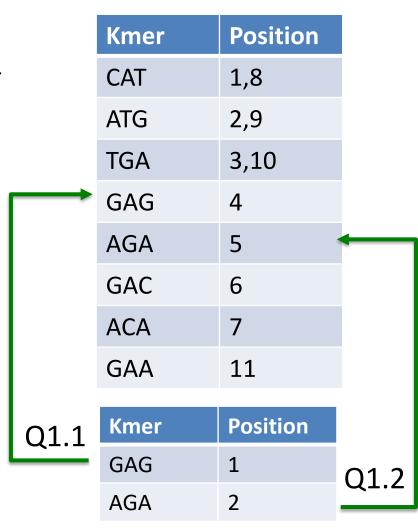
Searchstring: CATGAGACATGAA

Query1: GAGA

Query2: CATG

Query3: ATGT

- Decide on a word length k, e.g.,
   k=3
- 2) Build hash table from search string, storing every word occurring in S together with its start position.
- 3) Process query and search for each word occurring in Q1 whether it is in the hash table.
- 4) Repeat for Q2.



Two lookups are sufficient to find *Q1* in *S* 

#### Indexing handling mismatches?

2) How does the mapper deal with queries that 'almost' match the reference?

Q3 matches the reference with one mismatch

Relevant for sensitivity and specificity of the mapping.
Allowing more mismatches increases sensitivity (consider sequencing error and genetic diversity) but decreases specificity (more false positives).

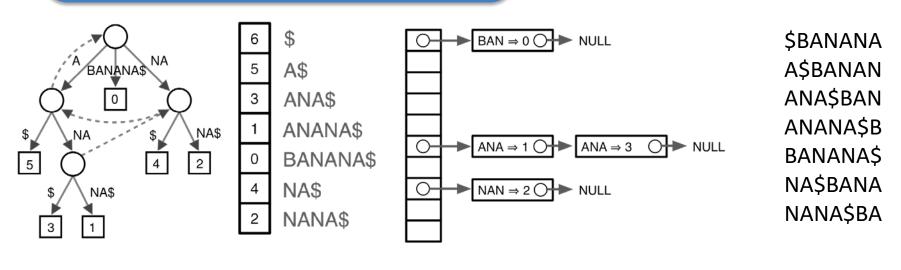
	Vmor	Docition	ı
	Kmer	Position	
	CAT	1,8	
	ATG	2,9	
	TGA	3,10	
	GAG	4	
	AGA	5	0
	GAC	6	ne
	ACA	7	One mismatch
	GAA	11	ma
tc			
Q3.1	Kmer	Position	<b>→</b>
20.2	ATG	1	
	TGT	2	

The 2<sup>nd</sup> lookup indicates that *Q3* is almost in *S* 

#### Main differences between mapping approaches

3) What kind of index does the mapper use?

Relevant for speed and memory footprint of the mapper



Suffix tree

**Suffix array** 

Seed hash tables

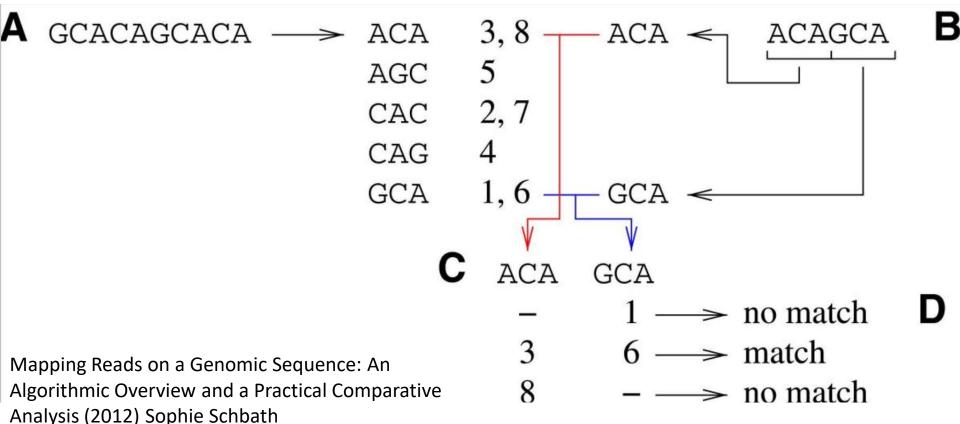
Many variants, incl. spaced seeds

**Burrows Wheeler Transformation** 

## **HASH-BASED MAPPING**

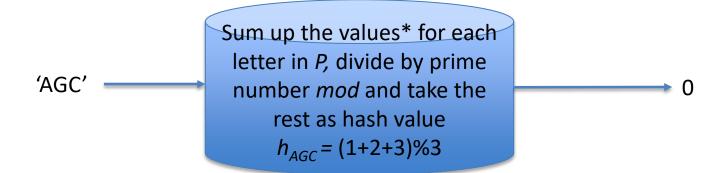
## The "traditional way": Hash tables

 Used by MAQ, Eland, SOAP, SHRiMP, ZOOM, partially by Mosaik, SSAHA2, Stampy



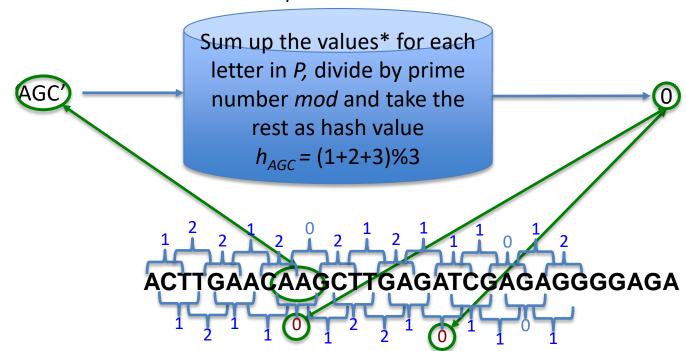
#### Approach:

1) Use a 'hash-function' to transform pattern P into a numerical hash value  $h_P$ .



#### Approach:

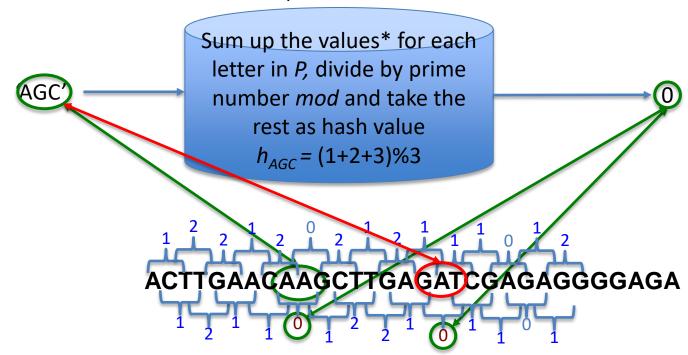
1) Use a 'hash-function' to transform pattern P into a numerical hash value  $h_P$ .



2) Search the text *T* starting from left for words of length *|P|* having the same hash value as *P*.

#### Approach:

1) Use a 'hash-function' to transform pattern P into a numerical hash value  $h_P$ .



2) Search the text *T* starting from left for words of length *|P|* having the same hash value as *P*.

#### Approach:

- 1) Use a 'hash-function' to transform pattern P into a numerical hash value  $h_P$ .
- 2) Search the text *T* starting from left for words of length *|P|* having the same hash value as *P*.
- 3) Given a word K with  $h_k = h_P$  was found, perform an exact string comparison to verify that K == P. (Note, the projection of words with length |P| in the space of hash values is **not** injective (linkseindeutig!).

'hashing' in combination with hash tables help to reduce the average time complexity of the pattern search to O(1), i.e. constant in time\*

#### Idea: Speed up pattern search by creating look-up tables storing the hash values

1) Search the text T starting from left for words of length k and compute their hash value  $h_k$ 



2) Store the hash values together with the starting point of the corresponding words in a hash table. Note, a hash table is nothing but a special way of indexing your data, just like a phone book. This will provide direct access to your potential matches in the pattern search once you know the hash value of *P*.

Hash value	Position in string
0	10,11,20,25,26
1	1,2,6,7,8, 12,15,18,19,21,22,23,24,27,28
2	3,4,5,9,13,14,16,17,29

<sup>\*</sup>note that this ignores the time and space you need to populate your hash table!

#### Seed and extend with local alignment

### SSAHA & Stampy:

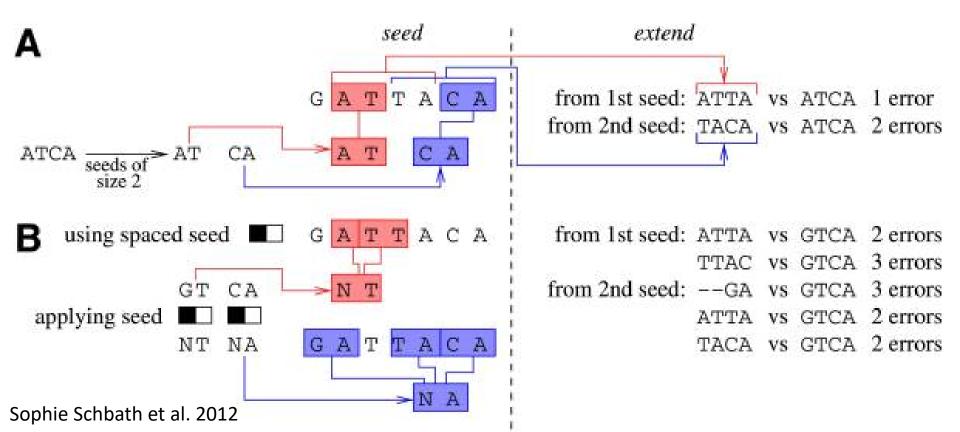
- Use k-mer (shorter than read) to find it in the genome
- Seed regions will be extended by Needleman-Wunsch

#### Drawback:

Many regions have to be analyzed in the extend phase

#### Seed and Extend the pigeon hole principle

- MAQ, SOAP, RMAP:
  - Chop read in k-mers (allowing errors)
  - All k-mers in the genome + correct order + adjacent to each other 
     read found



#### Seed and Extend the q-gram filtering

#### SHRiMP2 & RazerS:

- Chop read in k-mers but overlapping
- If enough k-mers map in a small region a more careful alignment will be done

#### • Drawback:

- List to large to be kept in memory
- Characters stored in 8 bits (2 bits per Nucleotide) but ambiguity code has to be overcome

# Why does MAQ\* use **pigeon hole principle** and **spaced seeds** for mapping?

Issues to solve by seed and extend:

- Shorter seeds map more regions on the genome
- Minimum of 10 nucleotides per k-mer
- Allowing "Don't care" positions to be able to find seeds 
   spaced seed approach

#### Reference

AGACTGAGGTACGTAGACCATGATCGATACCCAAAAAGCTAGA

**GTACGTAGACGATGATCCATACCCAAAA** 

Read (28 bp prefix)

MAQ uses seed pairs as it allows, per default no more than 2 mismatches between seed and reference. As each 28 mere is represented by 4 non-overlapping seeds, we always have at least 2 seeds that must result in a perfect match to the reference.

#### MAQ\*: pigeon hole principle for mapping

Example: read1 - gatgtgacatacctgttctactgaggct

Build **six** hash tables (templates) for the reads (only first 28 bp are considered) **only** from the colored nucleotides

6 'Templates'

gatgtgacatacctgttctactgaggct

→ 119777054

→ 2057673064
→ 773088662
→ 1856750201
→ 2510061809

hash value for template 1: 832589471

#### **GENOME**

compute hash values for spaced seeds in reference (on both strands and for one of the six templates) and perform lookups in hash tables of the reads

<sup>\*</sup>Li et al Genome Res. 2008. 18: 1851-1858

#### MAQ\*: pigeon hole principle for mapping

Example: read1 - gatgtgacatacctgttctactgaggct

Build **six** hash tables for the reads (only first 28 bp) using **only** the colored nucleotides

gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct → 2057673064

**→** 3178370917

**→** 773088662

→ 1856750201

**→** 2510061809

**→** 119777054

#### 1258119214

#### **GENOME**

continue with next word in the reference from the same template....

until the entire reference sequence has been used.

\*Li et al Genome Res. 2008. 18: 1851-1858

### MAQ \*: pigeon hole principle for mapping

Example: read1 - gatgtgacatacctgttctactgaggct

Build **six** hash tables for the reads (only first 28 bp) using **only** the colored nucleotides

**2057673064** 

gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct

→ 2057673064 → 3178370917 → 773088662 → 1856750201 → 2510061809

**→** 119777054

HIT: Calculate the sum of qualities of mismatched bases q over the whole length of the read and store together with hit position.

For each read, MAQ stores score and position of only the 2 best hits and the number of 0-, 1-, and 2-mismatch seed

positions

#### GENOME

\*Li et al Genome Res. 2008. 18: 1851-1858

Example: read1 - gatgtgacatacctgttctactgaggct

Build **six** hash tables for the reads (only first 28 bp) using **only** the colored nucleotides

gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct → 2057673064

→ 3178370917

**→** 773088662

→ 1856750201

**→** 2510061809

**→ 119777054** 

hash value for template 2

#### **GENOME**

Example: read1 - gatgtgacatacctgttctactgaggct

Build **six** hash tables for the reads (only first 28 bp) using **only** the colored nucleotides

gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct

→ 3178370917

→ 2057673064

**→** 773088662

→ 1856750201

**→** 2510061809

→ 119777054

hash value 3

#### **GENOME**

Example: read1 - gatgtgacatacctgttctactgaggct

Build **six** hash tables for the reads (only first 28 bp) using **only** the colored nucleotides

gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct

→ 2057673064

→ 3178370917

**→** 773088662

→ 1856750201

**2510061809** 

→ 119777054

hash value 4

#### **GENOME**

Example: read1 - gatgtgacatacctgttctactgaggct

Build **six** hash tables for the reads (only first 28 bp) using **only** the colored nucleotides

gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct gatgtgacatacctgttctactgaggct

→ 2057673064

→ 3178370917

**→** 773088662

→ 1856750201

**→** 2510061809

→ 119777054

hash value 5

#### **GENOME**

compute hash values for spaced seeds in reference (on both strands) and perform lookup in hash tables of the reads

Li et al Genome Res. 2008. 18: 1851-1858

Example: read1 - gatgtgacatacctgttctactgaggct

Build **six** hash tables for the reads (only first 28 bp) using **only** the colored nucleotides

gatgtgacatacctgttctactgaggct
gatgtgacatacctgttctactgaggct
gatgtgacatacctgttctactgaggct
gatgtgacatacctgttctactgaggct
gatgtgacatacctgttctactgaggct
gatgtgacatacctgttctactgaggct
gatgtgacatacctgttctactgaggct

→ 2057673064

→ 3178370917

**→** 773088662

→ 1856750201

**→** 2510061809

→ 119777054

hash value 6

#### **GENOME**

#### MAQ: An overview

- 1. At the alignment stage, MAQ first searches for the ungapped match with lowest mismatch score, defined as the sum of qualities at mismatching bases.
- 2. MAQ only considers positions that have two or fewer mismatches in the first 28 bp (default parameters; speed-up).
- Sequences that fail to reach a mismatch score threshold but whose mate pair is mapped are searched with a gapped alignment algorithm in the regions defined by the mate pair.
- 4. To evaluate the reliability of alignments, MAQ assigns each individual alignment a phred-scaled quality score (capped at 99), which measures the probability that the true alignment is not the one found by MAQ.
- 5. MAQ always reports a single alignment, and if a read can be aligned equally well to multiple positions, MAQ will randomly pick one position and give it a mapping quality zero. Because their mapping score is set to zero, reads that are mapped equally well to multiple positions will not contribute to variant calling.

#### NextGenMap

- Hash-based read mapper bridging:
  - 1. speed
  - 2. ability to map reads in highly polymorphic regions
- pitfalls:
  - Mixing single end and paired end reads is not supported → corrupt the mapping results
  - 2. Not recommended to change parameters –kmer and kmer-skip
  - 3. Values between 0.5 and 0.8 give the best trade-off between speed and sensitivity

### Algorithm Workflow

- Indexing the reference genome (only once)
- Identification of possible mapping regions on the reference genome (candidate mapping region (CMR) search)
- 3. Computation of alignment scores for all CMRs found in step 2
- 4. Computation of the full alignment for the best scoring CMR from step 3

### Indexing the reference genome

Key

AAAA

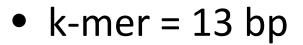
AAAC

AAAG

AAAT

TTTG

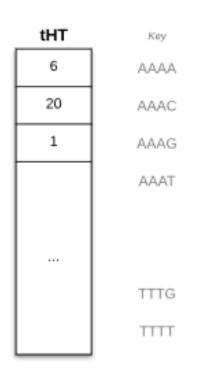
TTTT

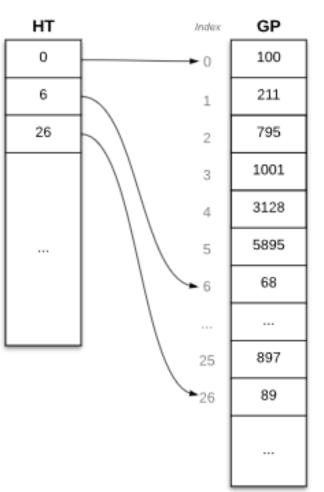


• Every 3. position

• Only A, C, G, T

Only + strand

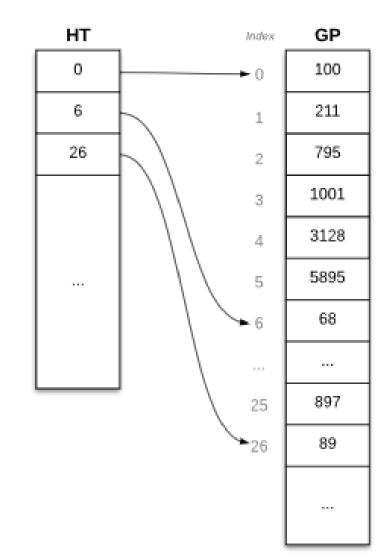




#### Indexing the reference genome

- GP = genomic positions
  - Consecutively k-mer blocks
  - Saving start position

- HT = Hash table of k-mers
  - Lexicographic ordered
  - Frequency (numbered serially)



Key

AAAA

AAAC

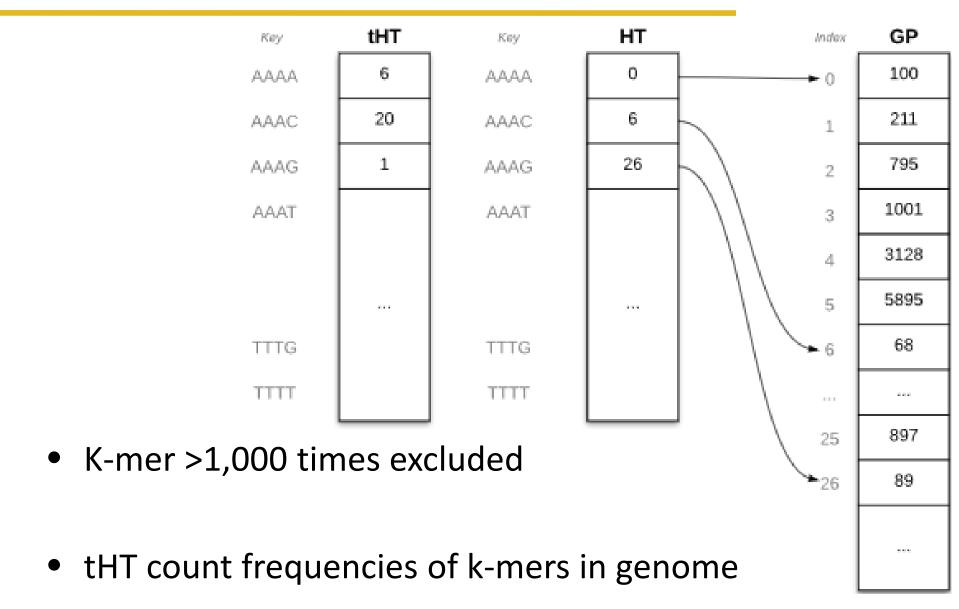
AAAG

AAAT

TTTG

TTTT

#### Indexing the reference genome



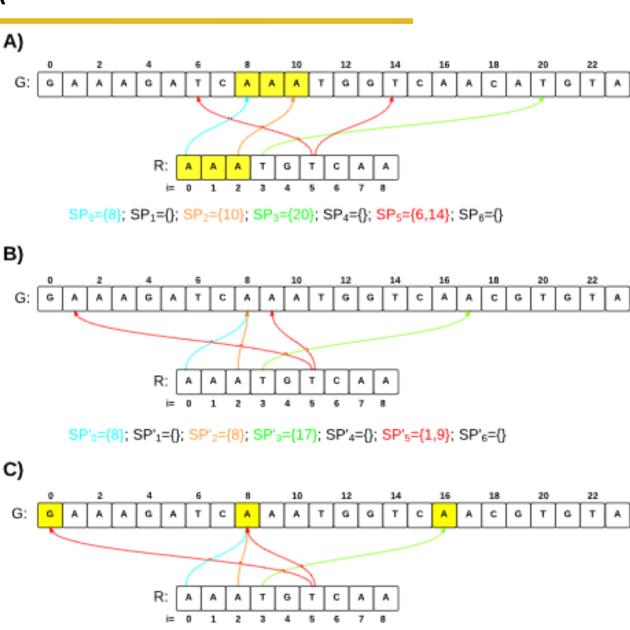
#### Identification of CMR

R = read of length9bp

G = referenceGenome

• Step-size = 2

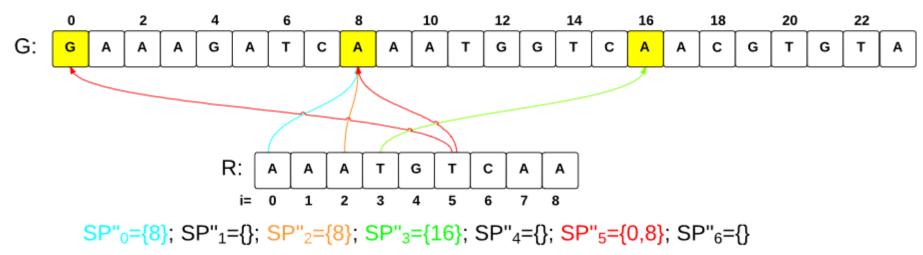
• k-mer size = 3bp



SP"<sub>0</sub>={8}; SP"<sub>1</sub>={}; SP"<sub>2</sub>={8}; SP"<sub>3</sub>={16}; SP"<sub>4</sub>={}; SP"<sub>5</sub>={0,8}; SP"<sub>6</sub>={}

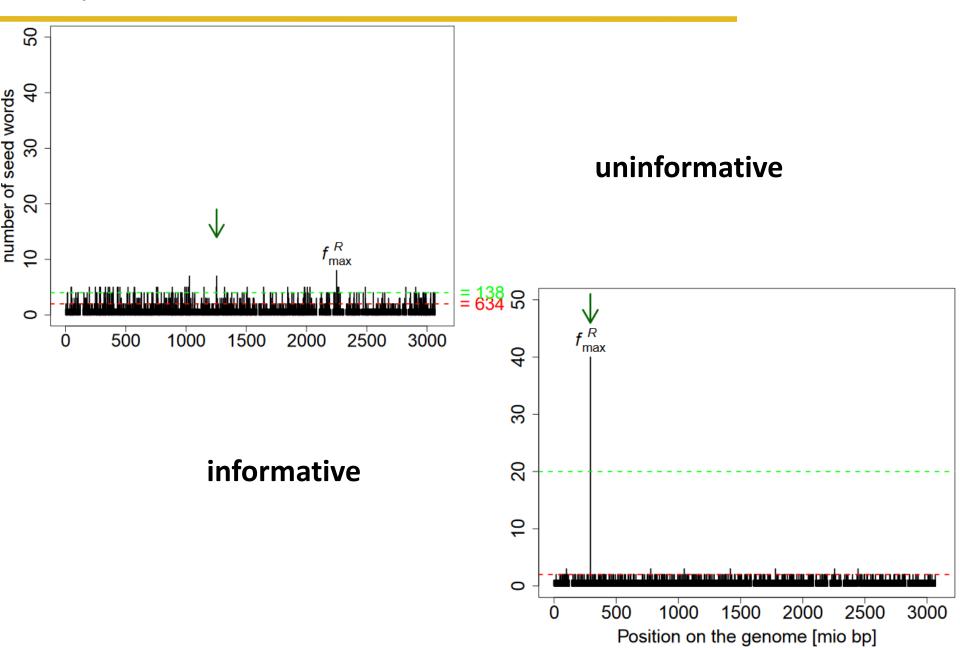
#### Identification of CMR





- Position 1 not found due to step-size =2
- Saving startpoints in reference genome
- Shift of readstart to startposition
- Allow modulo 8 (bit-shift operation) due to polymorphic regions to reduce start positions

#### Computation of CMRs





### **Computation of CMRs**

$$\sigma = \frac{\overline{F_{\text{max}}} = \frac{1}{B} \sum_{j=1}^{B} \max\{F_{R_j}\}}{S_{\text{max}} = \left\lceil \frac{l - k + 1}{\Delta} \right\rceil}$$

- Calculating the ratio of
  - Average read seed count
  - Perfectly matching read
- $\sigma = 1 \rightarrow \text{perfect reads}$
- $\sigma = 0 \rightarrow \text{very different reads}$
- Calculating genomic start points
  - $\rightarrow$  Frequency distribution
  - ightharpoonup Genomic position with seed word count above  $\Theta_R$

$$\Theta_R = \sigma \max\{F_R\}$$

#### Computation of alignment scores

- 1. Calculating the read alignment score p'' c/2 to p'' + l + c/2.
- 2. c defines consecutive insertions deletions dependent on the read length (I)  $c = 5 + \bar{l} * 0.15$
- 3. MASon (Rescheneder et al. 2012) for alignment

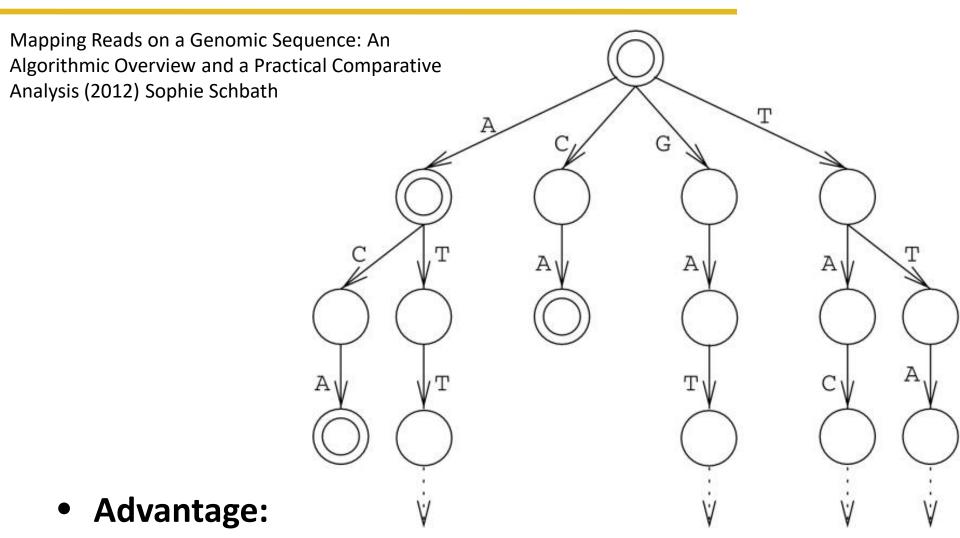
# BURROWS-WHEELER TRANSFORM BASED ALGORITHMS

#### Suffix Trees / Suffix Tries

- Advantage:
  - Hashing performs poor for repeating regions

- Each suffix of a word is represented as path from leave to root
  - Size of tree proportional to size of genome
  - Building time proportional to size of genome
  - Search time O(L<sub>r</sub>)

#### **Suffix Trees**



- Hashing performs poor for repeating regions
- Repeating regions are squeezed into one path

#### **Suffix Arrays**

- Problem of the trees and tries:
  - Large genomes will not fit in the RAM
- Array is the set of suffixes sorted lexicographically
  - Trick 1: save the startposition of the suffix

genome	suffixes	sorted suffixes	positions	cylinder suffix array	$\mathrm{B}\text{-}\mathrm{W}$
GATTACA\$	GATTACA\$	ACA\$	4	ACA\$GATT	T
And the state of t	ATTACA\$	ATTACA\$	2	ATTACA\$G	G
	TTACA\$	A\$	6	A\$GATTAC	C
	TACA\$	CA\$	5	CA\$GATTA	Α
	ACA\$	GATTACA\$	1	GATTACA\$	\$
	CA\$	TACA\$	4	TACA\$GAT	T
	A\$	TTACA\$	3	TTACA\$GA	Α
	\$	\$	7	\$GATTACA	Α

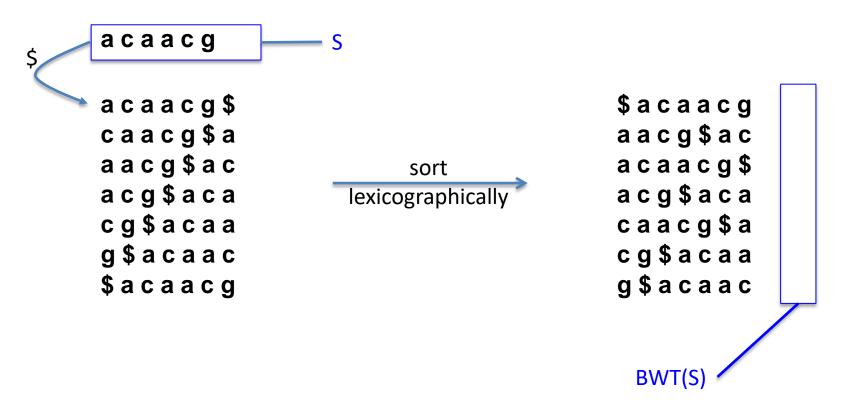
Mapping Reads on a Genomic Sequence: An Algorithmic Overview and a Practical Comparative Analysis

(2012) Sophie Schbath

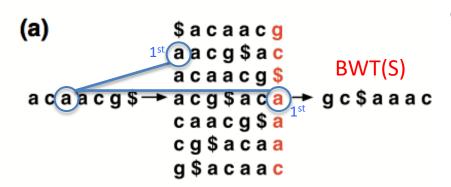
#### Trick 2: The Burrows-Wheeler Transform

- Invented by David Wheeler in 1983 (bell labs), pub.
   1994
- Used in data compression (bzip2)
- Used in 2003 on the human genome to define exact word matches (originally for microarray probe design)
- First used for short read alignment by bowtie, now adopted by bwa (maq author) and SOAP2

#### The Burrows-Wheeler Transform



#### Burrows Wheeler Transform (BWT)

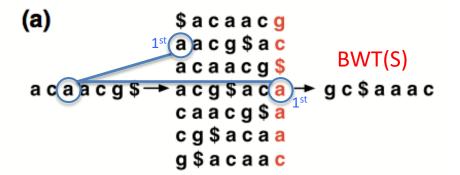


Generate matrix by

- 1. Appending a \$\\$ to the end of the string \$S\$ that should be indexed. \$\\$ should have 2 properties
  - 1. it must not occur in the string
  - 2. it should be lexicographically smaller than any character in S
- 2. generate all cyclic permutations of S
- 3. sort the resulting matrix lexicographically (the line beginning with the \$ is the first to occur in the matrix.

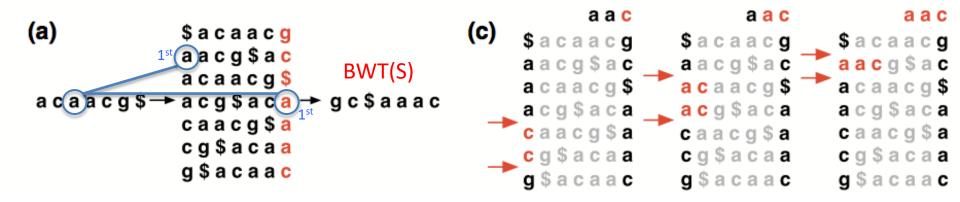
The matrix has the property of last first (LF) mapping: The ith occurrence of character X in the last column corresponds to the same text character as the ith occurrence of X in the first column

#### **Burrows Wheeler Transform (BWT)**



The matrix has the property of last first (LF) mapping: This can be used to reconstruct the original text from BWT(S) using the UNPERMUTE algorithm.

#### **Burrows Wheeler Transform (BWT)**



The matrix has the property of last first (LF) mapping: This can be used to search for a text within BWT(S) using the EXACTMATCH algorithm. Key aspects:

- 1) Matrix is sorted lexicographically. Thus, rows beginning with a given sequence appear **consecutively**.
- 2) EXACTMATCH algorithm calculates the range of matrix rows beginning with **successively longer suffixes** of the query.
- 3) At each step, the size of the range either shrinks or remains the same.
- 4) When the algorithm completes, rows beginning with S<sub>0</sub> (the entire query) correspond to exact occurrences of the query in the text.

# Original string: ctgaaactggt Put a \$ on the end create cyclic rotations of the string...

```
t
g
            а
                 С
                         g
                         g
а
            С
                              $
                         t
                                      t
а
            t
                g
                    g
                         $
а
    С
            g
                g
                   t
                             С
                                  t
                                      g
                    $
                t
                         С
С
            g
                                 g
                                      а
                                              а
                $
t
                         t
            t
                    С
                             g
g
                 С
                    t
                         g
                             а
                                      а
            С
                     g
                         а
                             а
t
            t
                g
                         а
    С
            g
                     а
                         а
                              С
                                      g
                 а
```

Alphabetically sort the permuted strings, first column is the "genome dictionary" last column is the Burrows-wheeler transformation

\$						t	11
a						g	3
a						a	4
a						a	5
C						\$	0
C						a	6
g						t	2
g						t	8
g						g	9
t						g	10
t						C	1
t						C	7

Look up ctgg: start at the end with g, lookup in genome dictionary

top(g) = 6; bot(g) = 8

```
0
 3
 4
 5
 6
 8
10
11
                                                                C
```

Does gg exist, and what are top(gg) and bot(gg)? Yes, gg exists.

```
top(gg) = top(g) + #g before g-block in bwt = 6 + 1 = 7
bot(gg) = top(gg) + # of gg in genome -1 = 7 + 1 - 1 = 7
```

```
t
                           q
                                    $
                      g
 4
                       а
 5
                                $
                                    С
                       g
                                                            a
 6
                                    g
                                                            t
                       $
 8
                       C
                                    а
                                                            g
 9
10
                                    t
11
                                C
                                                            C
```

Does tgg exist, and what are top(tgg) and bot(tgg)? Yes, tgg exists.

```
top(tgg) = top(t) + \#t before gg-block in bwt = 9 + 2 = 11
bot(tgg) = top(tgg) + \# of tgg in genome -1 = 11 + 1 - 1 = 11
```

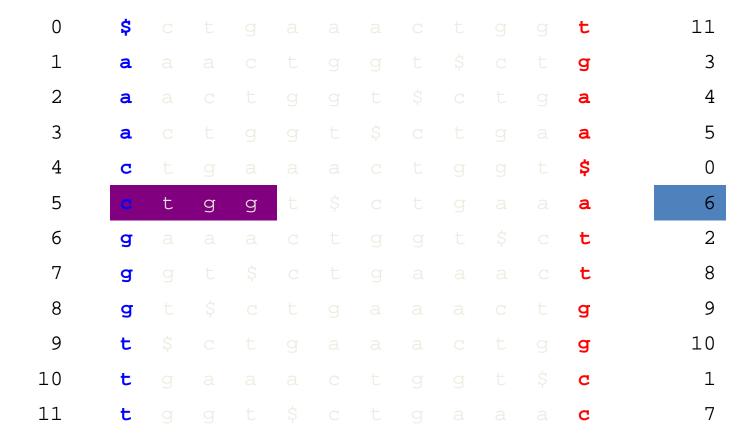
```
0
                              g
                   t
                       q
                              t
 3
                       g t
                              $
                   g
 4
                   а
                                      g
 5
                       t
                              С
 6
                              g
                   $
                              g
 8
                   C
 9
                   t
                       q
                              а
                                                  g
10
                             t
11
```

Does ctgg exist, and what are top(ctgg) and bot(ctgg)? Yes, ctgg exists.

```
top(ctgg) = top(c) + #c before tgg-block in bwt = 4 + 1 = 5
bot(ctgg) = top(ctgg) + # of ctgg in genome -1 = 5 + 1 - 1 = 5
```

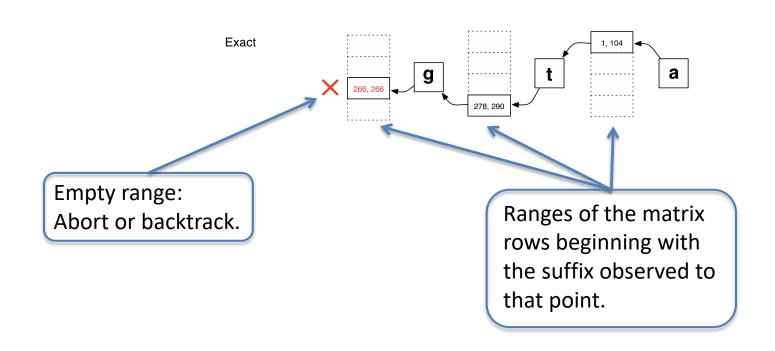
```
0
            $
                                                                              t
  3
                                               $
  4
 5
                             g
                                               C
 6
                                                g
 8
                             С
10
11
                             t
                                                                              C
                                         \mathsf{C}
```

# Found ctgg at position 5, which is position 6 in original string ctgaaactggt



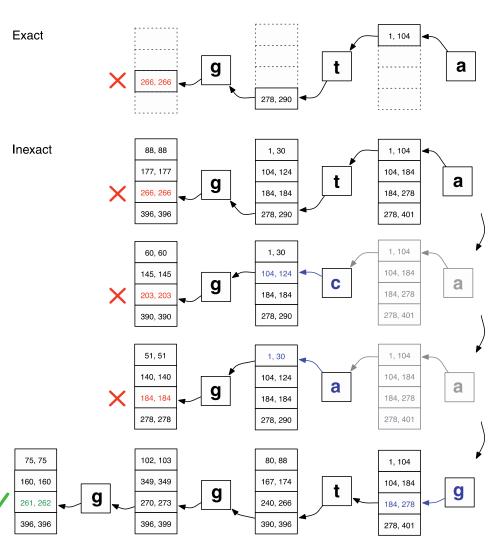


## Coping with mismatches: Query GGTA





# Quality-aware, greedy, randomized, depth-first search through the space of possible alignments.



- 1. The search proceeds similarly to EXACTMATCH
- If range becomes empty (suffix does not occur in text), the algorithm backtracks and selects an already-matched query position and substitutes a different base there. The EXACTMATCH algorithm resumes from this modified position.
- 3. The algorithm allows only substitutions that yield a modified suffix that occurs at least once in the text. If there are multiple candidate substitution positions, then the algorithm greedily selects a position with a minimal quality value.
- Because search is greedy, the first valid alignment is not necessarily the best (Number of mismatches and quality).
   Bowtie has parameters to cope with this (--best or –all (all alignments).
- 5. Excessive Backtracking should be avoided. Note, we start from the low quality end...

#### Coping with mismatches

- Our alignment policy allows a limited number of mismatches and prefers alignments where the sum of the quality values at all mismatched positions is low.
- The search proceeds similarly to EXACTMATCH, calculating matrix ranges for successively longer query suffixes.
- If the range becomes empty (a suffix does not occur in the text), then the
  algorithm may select an already-matched query position and substitute a
  different base there. The EXACTMATCH algorithm resumes from this
  position.
- The algorithm selects only those substitutions that yield a modified suffix that occurs at least once in the text. If there are multiple candidate substitution positions, then the algorithm greedily selects a position with a minimal quality value.

# Bowtie: Avoidance of excessive backtracking (assuming 1 mismatch)

**Problem:** The aligner spends most of its effort fruitlessly backtracking to positions close to the 3' end of the query (error prone).

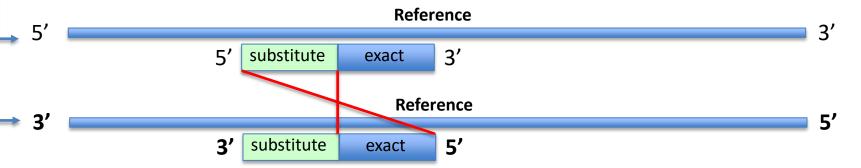
Solution Part1: double indexing (similar to MAQ), using two indices for the genome

- Index 1: BWT of the original genome
- Index 2: BWT of the genome with reversed character order (not reverse complemented!)

**Solution Part2:** The aligner is invoked twice

- First round: Index 1 is used, and the aligner is started with original read with the constraint that it must not substitute a position in the query's right half (3' end).
- Second round: Index 2 is used, and the aligner is started with the reversed read, again with the constraint that it must not substitute a position in the reversed query's right half (originally and still the 5' end).

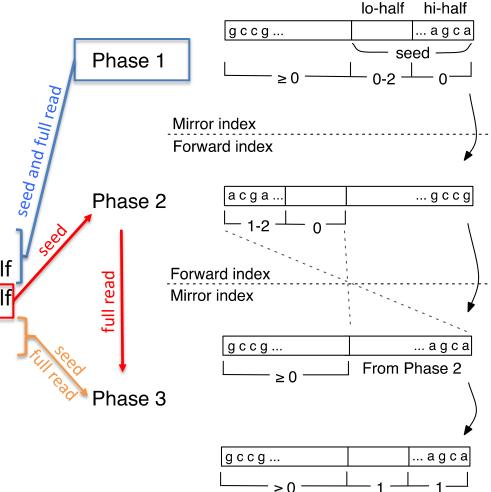
**Solution Part3:** set a hard upper limit of backtracks to be performed.



#### The three phases of Bowtie

#### In the case of 2 (or more mismatches):

- Bowtie uses the first 28 bp as seed
- The seed is split into a high quality 5' half (hi-half) and a low quality 3' half (lo-half)
- For up to 2 mismatches we have four scenarios:
  - 1. no mismatches in seed
  - 2. 1-2 mismatches only in the lo-half
  - 3. 1-2 mismatches only in the hi-half
  - 4. 1 mismatch each in hi- and lowhalf
- Any number of mismatches can occur in non-seed part (subject to other thresholds).



#### Changes in Bowtie2

Supports gapped, local, and paired-end alignment modes:

- For reads longer than about 50 bp Bowtie 2 is generally faster, more sensitive, and uses less memory.
- Bowtie 2 supports <u>local alignment</u>, which doesn't require reads to align end-to-end. Local alignments might be "trimmed" ("soft clipped") at one or both extremes in a way that optimizes alignment score.
- There is no upper limit on read length in Bowtie 2.
- Bowtie 2 allows alignments to <u>overlap ambiguous</u> characters (e.g. Ns) in the reference.

#### Bowtie2: Seed extraction & alignment

#### **Seed extraction:**

- Substrings of the read ("seed strings") are extracted at regular intervals along the read and its reverse complement.
- Seed strings are contiguous (i.e. they are not spaced seeds) and may or may not overlap each other.

#### FM Index assisted seed alignment:

- Find ungapped alignments for each based on Bowtie1
- Seed strings can be aligned with up to 1 mismatch.

### Bowtie2: Seed alignment priorization & alignment

#### **Priorization:**

- "seed-hit range" → A seed-hit range describes a range of rows in the Burrows-Wheeler matrix that begin with a reference substring that is within 0 or 1 mismatches of the seed substring.
- Bowtie 2 proceeds by repeatedly selecting a row in a random weighted fashion using these weights.

#### **Alignment:**

- Bowtie 2 extracts flanking characters from the reference
- Solves a rectangular dynamic programming problem to find high-scoring full alignments in the vicinity of the seed hit.



### Watch out for the following...

- Up to 2 mismatches in first 28 bases reported by Maq (default) and 1-2 mismatches by Bowtie1/2 in the seed.
- If >=1 matching seed regions exist for one read Bowtie2 has a dynamic programming effort limit of 15. After 15 attempts not performing better than the best so far.
- Bowtie outperforms Bowtie2 in case of short reads (<=50 nt) in some cases.</li>
- Bowtie convert N to A, C, G or T randomly / Bowtie2 accepts N's

